## (11) Plane Geometry

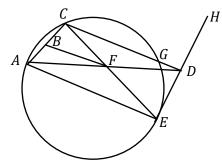
1. In the figure (not drawn to scale), *AE* is the diameter of the circle, *F* is the mid-point of *CE* and *ED* is tangent to the circle at *E*. *CG*, *BF* and *AE* are parallel lines.

a) Prove that  $\triangle ACE$  is congruent to  $\triangle EDC$ 

b) Prove that CBF is similar to DEC

c) Prove that  $CD \times CE = 4CF \times BF$ 

d) Prove that  $AE^2 = CA^2 + CD^2 + DE^2$ 

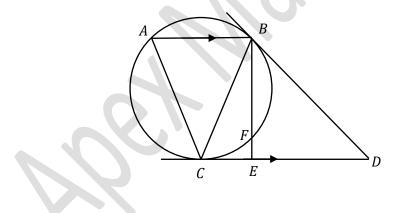


2. In the figure, *BD* and *CD* are tangents to the circle at *B* and *C* respectively. *AB* is parallel to *CD* and *BE* is perpendicular to *CD*.

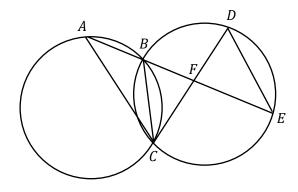
a) Prove that ABC is an isosceles triangle

b) Prove that  $\Delta DCB$  is similar to  $\Delta CAB$ 

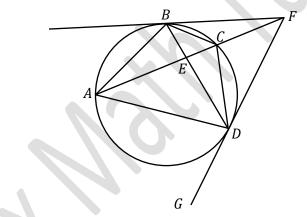
c) Prove that  $CE^2 + EB^2 = AB \times DB$ 



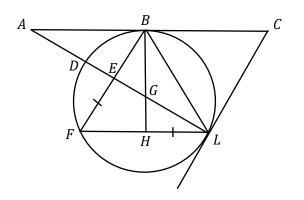
- 3. In the diagram, CD is a tangent to the circle ABC at C. BC is a common chord between both circles and F is the intersection between lines AE and CD.
  - a) Prove that AC is parallel to DE.
  - b) Prove that  $CF^2 = AF \times FB$



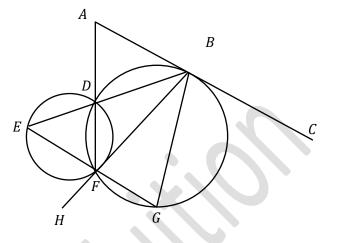
4. In the diagram, BD and DF are tangents to the circle and  $\angle ABD = 2 \angle DBC$ . Prove that AD = DF.



5. *BCF* is an equilateral triangle inscribed in a circle. *ABC* is a tangent to the circle at point *B*. Given that EF = HL and *AEGL* is a straight line, prove that



- 6. In the diagram, the 2 circles intersect at points *D* and *F*. *ABC* is a tangent to the bigger circle at *B* and *HFB* is a tangent to the smaller circle at *F*. *ADF*, *EDB* and *EFG* are straight lines.
  - a) Prove that BF = BG.
  - b) Show that ABC is parallel to EFG
  - c) Show that  $\Delta BDA$  is similar to  $\Delta EGB$

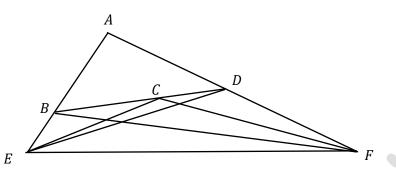


7. In the diagram, B is the mid-point of AC and G is the midpoint of AD. CDE and BGF are straight lines. Given that BH = 2HE, show that,
a) ΔDHE is similar to ΔGHB
b) AH = 5DH

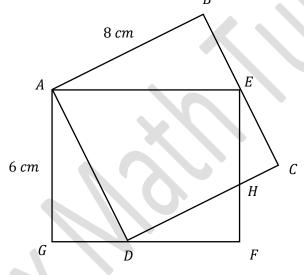
D Ε С

8. The diagram shows triangle *AEF* where AD = DF, AB = 2BE and BC = 3CD. Find the value of <u>Area of  $\Delta CDE</u>$ .</u>





9. In the figure, *ABCD* is a square with sides 8 cm and *AEFG* is a rectangle. Given that AG = 6cm, find the length of *GF*.



10. In the diagram, AFE is a triangle inscribed in a circle. ABCD is a parallelogram and AB is a tangent to the circle at point A. Prove that

