## (11) Plane Geometry

1. In the figure (not drawn to scale), $A E$ is the diameter of the circle, $F$ is the mid-point of $C E$ and $E D$ is tangent to the circle at $E . C G, B F$ and $A E$ are parallel lines.
a) Prove that $\triangle A C E$ is congruent to $\triangle E D C$
b) Prove that $C B F$ is similar to $D E C$
c) Prove that $C D \times C E=4 C F \times B F$
d) Prove that $A E^{2}=C A^{2}+C D^{2}+D E^{2}$

2. In the figure, $B D$ and $C D$ are tangents to the circle at $B$ and $C$ respectively. $A B$ is parallel to $C D$ and $B E$ is perpendicular to $C D$.
a) Prove that $A B C$ is an isosceles triangle
b) Prove that $\triangle D C B$ is similar to $\triangle C A B$
c) Prove that $C E^{2}+E B^{2}=A B \times D B$

3. In the diagram, $C D$ is a tangent to the circle $A B C$ at $C . B C$ is a common chord between both circles and $F$ is the intersection between lines $A E$ and $C D$.
a) Prove that $A C$ is parallel to $D E$.
b) Prove that $C F^{2}=A F \times F B$

4. In the diagram, BD and DF are tangents to the circle and $\Varangle A B D=2 \Varangle D B C$. Prove that $A D=$ $D F$.

5. $B C F$ is an equilateral triangle inscribed in a circle. $A B C$ is a tangent to the circle at point $B$. Given that $E F=H L$ and $A E G L$ is a straight line, prove that

6. In the diagram, the 2 circles intersect at points $D$ and $F . A B C$ is a tangent to the bigger circle at $B$ and $H F B$ is a tangent to the smaller circle at $F . A D F, E D B$ and $E F G$ are straight lines.
a) Prove that $B F=B G$.
b) Show that $A B C$ is parallel to $E F G$
c) Show that $\triangle B D A$ is similar to $\triangle E G B$

7. In the diagram, $B$ is the mid-point of $A C$ and $G$ is the midpoint of $A D . C D E$ and $B G F$ are straight lines. Given that $B H=2 H E$, show that,
a) $\triangle D H E$ is similar to $\triangle G H B$
b) $A H=5 D H$

8. The diagram shows triangle $A E F$ where $A D=D F, A B=2 B E$ and $B C=3 C D$. Find the value of $\frac{\text { Area of } \triangle C D E}{\text { Area of } \triangle A E F}$.

9. In the figure, $A B C D$ is a square with sides 8 cm and $A E F G$ is a rectangle. Given that $A G=6 \mathrm{~cm}$, find the length of $G F$.

10. In the diagram, $A F E$ is a triangle inscribed in a circle. $A B C D$ is a parallelogram and $A B$ is a tangent to the circle at point $A$. Prove that

