

## (5) Modulus and Graph of Logarithms/Exponentials Functions

1. Sketch the graph  $y = e^{x+2}$ . State the equation of a straight line that can be drawn to solve the equation  $x + 2 = \ln(x + 1) - \ln 2$ .

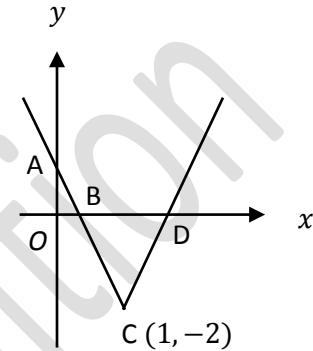
2. The figure shows part of the graph of  $y = |ax - 4| + b$  where  $C(1, -2)$  is the minimum point of the graph.

i) State the value of  $b$

ii) Find the value of  $a$

iii) Find the coordinates of  $A$ ,  $B$  and  $D$ .

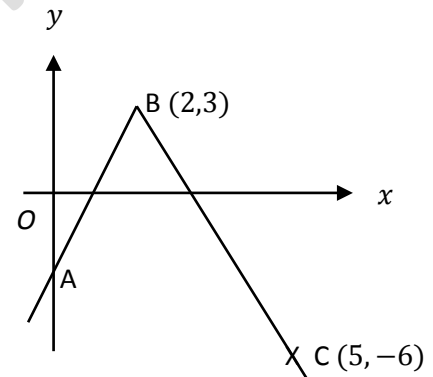
iv) Write down the range of values of  $x$  for which  $y$  is negative.



3. The diagram show part of the graph of  $y = a - |bx + c|$  where  $b > 0$ . Given that it passes through the points  $B(2,3)$  and  $C(5, -6)$ ,

i) Find the values of  $a$ ,  $b$  and  $c$

ii) Find the  $x$ -intercepts and the  $y$ -intercept of the graph.

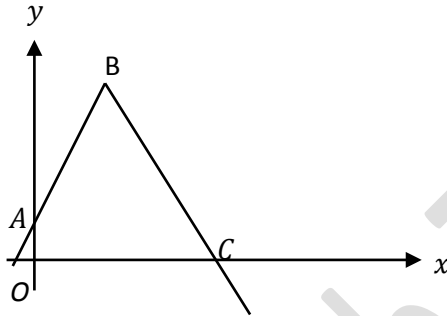


4. Sketch the graph  $y = 3 \ln(x + 1)$ . On the same graph, add a suitable straight line which will help solve the equation  $(x + 1)e^{\frac{1}{3}x+1} = e^2$ . State the equation of the straight line.
5. Solve the equation  $|-3x + 21| = 8x + |x - 7|$

6. i) On the same diagram, sketch the graphs of  $y = |2x|$  and  $y = |x + 3|$ .  
 ii) State the number of solutions of the equation for  $|2x| = |x + 3|$ .  
 iii) Find the coordinates of the intersection points of the 2 graphs.  
 iv) Hence, state the solution of  $|2x| > |x + 3|$ .

7. a) Solve the equation  $|x - 2| = 2 - 4x$

b) The diagram shows part of the graph of  $y = 4 - |2x - 3|$ . Find the coordinates of  $A, B$  and  $C$ .



8.  $|2x^2 + 4x - 11| > 5$

9. i) Sketch the graph  $y = |x^2 - 2x|$  indicating the intercepts and coordinates of the turning point.

ii) In each of the following case, determine the number of solutions of the equation  $|x^2 - 2x| = mx + c$  where  $0 < c < 1$ , justify your answer.

a)  $m = 0$

b)  $m = -1$

10. i) Sketch the graph of  $y = |3x - 2|$  for  $-1 < x < 2$ .

ii) State the corresponding range of  $y$ .

iii) Find the range of values of  $c$  for which  $|3x - 2| = 3x + c$  has only one solution for  $-1 < x < 3$ .